

Primary Maths **PROBLEMS** *for* **6-8** year olds

- * **Task cards for developing a range of maths problem solving strategies.**
- * **Activities cover all key learning areas of the maths curriculum.**

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Introduction

The **Primary Maths Problems** series is a comprehensive teacher resource containing a variety of reproducible mathematical problem task cards – some with one solution, some with a number of solutions and some open ended. The problems are related to practical everyday mathematical situations, with each activity designed to challenge students to use their knowledge and problem solving skills.

Problem solving can develop many valuable skills in our students such as logical reasoning, creative thinking and communication skills. Students require perseverance, flexibility in ideas and methods, reflective thinking and confidence if they are going to be successful in this area. The problems will ask students to draw on a number of mathematical strategies in order to solve them. These strategies need to be introduced and taught to students if they are going to gain the skills necessary to solve a variety of problems. For students to solve a problem they first need to read the facts carefully and understand what the problem is asking them to do. They then need to work out a plan for solving the problem, carry out the processes involved and hopefully look back over their answer and assess the results successfully.

Problems can be solved using a number of different strategies. These strategies may include:

- Think, estimate and check
- Draw a diagram or picture
- Look for patterns
- Make a model
- Act out the problem
- Construct a table or a graph
- Write a statement
- Make a list
- Calculate
- Reflect and assess results

Prior to presenting the problems from this book to your students, put a list of these strategies on display. Go through each one and present students with an example to work with. Keep the strategies on display, then as your students work through the various problem cards from this book, ask them which strategies they need to solve each problem. In some cases they may need to use more than one strategy to solve a problem. A checklist included in this book allows teachers and students to keep a record of the strategies used to solve each problem. The above strategies are explained more thoroughly and with examples further on in the teaching notes, which ideally should be worked through with the students.

The problem cards in this book have been divided into the four main areas of the maths curriculum:

- SPACE
- NUMBER
- MEASUREMENT
- CHANCE and DATA

The principles of WORKING MATHEMATICALLY and REASONING and STRATEGIES have been incorporated into each of the four main areas.

Contents

Introduction
 Contents and Curriculum Links
 Teachers' Notes
 Teaching Points and Examples
 Assessment Checklist

... page 2
 ... page 3
 ... page 8
 ... page 9
 ... page 13

PROBLEM CARDS: Space and Location

TITLE	STRATEGY	OUTCOME	PAGE #
Task 1: Shape Pictures	Draw a picture	Constructs recognisable pictures from 2D shapes.	page 14
Task 2: Coins	Look for patterns Make a model	Orders a shape according to size and makes a 3D shape from a 2D shape.	page 14
Task 3: Tables and Chairs	Make a model	Uses shape blocks to construct recognisable objects.	page 15
Task 4: Cube	Make a model	Identifies and constructs a 3D shape from a 2D shape.	page 15
Task 5: Towers	Act it out	Compares 3D shapes when using them to construct things.	page 16
Task 6: Fruit and Vegetables	Estimate and check Make a list	Names and recognises the uses for common 3D shapes.	page 16
Task 7: Shape Patterns	Look for patterns	Makes simple patterns using shapes from a set of instructions.	page 17
Task 8: Brick Wall	Look for patterns	Identifies and creates a simple repetitive pattern. Recognises useful shapes in construction.	page 17
Task 9: City of Shapes	Make a list Make a design	Identifies where familiar shapes are used in everyday life.	page 18
Task 10: Missing Half	Draw a picture	Uses shape and symmetry to complete and design simple pictures.	page 18
Task 11: Paving	Look for patterns Draw a picture	Identifies and uses shapes that can make a tessellating pattern.	page 19
Task 12: Shape Pictures	Draw a picture	Uses given shapes to create simple pictures.	page 19
Task 13: Classroom Paths	Act it out Draw a diagram	Moves and creates paths in response to simple instructions.	page 20
Task 14: Classroom Position	Write a statement	Uses location words to describe familiar positions.	page 20
Task 15: Left and Right	Draw a picture	Uses left and right to draw the position of objects.	page 21
Task 16: Bus Line	Draw a diagram	Uses left and right to describe the position of people.	page 21
Task 17: Creating Paths	Draw a diagram Write a statement	Creates different paths on a simple map.	page 22
Task 18: Possum Maze	Look for patterns	Locates and follows different paths on a maze.	page 22
Task 19: Board Game	Make a design	Designs and creates a simple board game.	page 23
Task 20: Bedroom Plans	Draw a diagram	Interprets and creates simple maps of familiar locations.	page 23
Task 21: Assessment: Bridges	Make a model	Identifies and uses shapes to construct a specific object.	page 24
Task 22: Assessment: Class Map	Draw a diagram Act it out	Interprets and creates simple maps of familiar locations.	page 24

PROBLEM CARDS: Number

TITLE	STRATEGY	OUTCOME	PAGE #
Task 1: Jack's Party	Look for patterns	Skip counts by different numbers to solve a problem	page 25
Task 2: Swap Cards	Calculate	Skip counts, adds and subtracts to solve a problem.	page 25
Task 3: Car Collection	Calculate	Doubles and halves numbers to solve a problem.	page 26
Task 4: Rebecca's Age	Estimate and check	Doubles and halves numbers to solve a problem.	page 26
Task 5: Street Numbers	Look for patterns Calculate	Uses odd and even numbers to solve a problem.	page 27
Task 6: Number Totals	Look for patterns Calculate	Calculates mentally numbers to 10.	page 27
Task 7: Ball Toss	Calculate	Uses addition and multiplication facts to solve a problem.	page 28
Task 8: Bowling	Calculate	Uses addition and multiplication facts to solve a problem.	page 28
Task 9: Street Signs	Look for patterns Draw a picture	Uses knowledge of number and counting to solve a problem.	page 29
Task 10: Farmers and Cows	Draw a picture Look for patterns	Uses knowledge of number and counting to solve a problem.	page 29

Curriculum Links

The activities in this book can be linked to the following areas in the Mathematics curriculum documents.

VICTORIA*

Levels 1-2

Number

Level 1: 1.1, 1.2, 1.3, 1.4, 1.5

Level 2:

Numbers, Counting and Numeration – 2.1, 2.2, 2.3, 2.4

Mental Computation and Estimation – 2.1

Computation and Applying Number – 2.1, 2.2, 2.3, 2.4

Number Patterns and Relationships – 2.1, 2.3

Space

Level 1: 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7

Level 2: Shape and Space – 2.1, 2.3, 2.4, 2.5, 2.6

Location – 2.1, 2.2, 2.3, 2.4

Measurement and Data

Level 1: 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7

Level 2:

Measuring and Estimating – 2.1, 2.3, 2.4, 2.5

Time – 2.1, 2.2

Using Relationships – 2.1

Chance – 2.1, 2.2

Data – 2.1, 2.2, 2.3, 2.4

Reasoning and Strategies

Level 1: 1.1, 1.2, 1.3

Level 2:

Mathematical Reasoning – 2.3, 2.3, 2.4

Strategies for Investigation – 2.1, 2.2

* *Incorporates VELS: Number, Space, Measurement, Chance and Data and Working Mathematically.*

SOUTH AUSTRALIA

Levels 1-2

Exploring, Analysing and Modelling Data – 1.1, 1.2, 1.3, 2.1, 2.2, 2.3

Measurement –

1.4, 1.5, 2.4, 2.5

Number –

1.6, 1.7, 1.8, 2.6, 2.7, 2.8

Pattern and Algebraic Reasoning –

1.9, 1.10, 1.11, 2.9, 2.10, 2.11

Spatial Sense and Geometric Reasoning –

1.12, 1.13, 1.14, 2.12, 2.13, 2.14

WESTERN AUSTRALIA

Levels 1-2

Working Mathematically

Contextualise Mathematics – WM 1.1, WM 2.1

Mathematical Strategies – WM 1.2, WM 2.2

Reason Mathematically – WM 1.3, WM 2.3

Apply and Verify – WM 1.4, WM 2.4

Space

Represent Location – S 1.1, S 2.1

Represent Shape – S 1.2, S 2.2

Represent Transformations – S 1.3, S 2.3

Reason Geometrically – S 1.4, S 2.4

Measurement

Understand Units – M 1.1, M 2.1

Direct Measure – M 1.2, M 2.2

Estimate – M 1.3, M 2.3

Indirect Measure – M 1.4, M 2.4

Chance and Data

Understand Chance – C&D 1.1, 2.1

Collect and Organise Data – C&D 1.2, 2.2

Summarise and Represent Data – C&D 1.3, 2.3

Interpret Data – C&D 1.4, 2.4

Number

Understand Numbers – N 1.1, N 2.1

Understand Operations – N 1.2, N 2.2

Calculate – N 1.3, N 2.3

Reason About Number Patterns – N 1.4, N 2.4

NEW SOUTH WALES

Levels 1-2

Working Mathematically

Questioning – WMS 1.1, WMS 2.1

Applying Strategies – WMS 1.2, WMS 2.2

Communicating – WMS 1.3, WMS 2.3

Reasoning – WMS 1.4, WMS 2.4

Reflecting – WMS 1.5, WMS 2.5

Number

Whole Numbers – NS 1.1, NS 2.1

Addition and Subtraction – NS 1.2, NS 2.2

Multiplication and Division – NS 1.3, NS 2.3

Fractions and Decimals – NS 1.4, NS 2.4

Chance – NS 1.5, NS 2.5

Teaching Points

PROBLEM SOLVING STRATEGIES

Think, estimate and check

This skill is often used subconsciously in problem solving as well as many other areas of maths. It should be the first step taken whenever a student is presented with a problem. Students read the problem at least once, think about what it is asking of them, estimate an answer and then check to see if they are correct. While solving a problem using this method, students may still need to work through a number of other strategies, such as calculating mentally or writing notes or sums, drawing up a table or chart or even checking using mathematical tools such as a calculator, scales, ruler and so on.

Example:

At the local fair there is a stall where you are given ten beanbags to throw into a bin two metres away. If you had three turns, how many beanbags do you think you are likely to get into the bin on the:

a) first turn?

b) second turn?

c) third turn?

Step 1: Read the problem and work out what it is asking?

Step 2: Think about and estimate how many beanbags you think you could throw into a bin. Do you think you would improve on the second and third try? You may even wish to check your answers by acting out the problem with actual beanbags and a bin if you have the equipment.

Step 3: Answers will vary from student to student depending on how confident they feel about throwing something into a target. If students do act out the problem, they would then need to check their estimates and see how close they were to how they performed. As this is a chance experiment, would the results be the same each time? *(Follow with class discussion.)*

Draw a diagram/picture

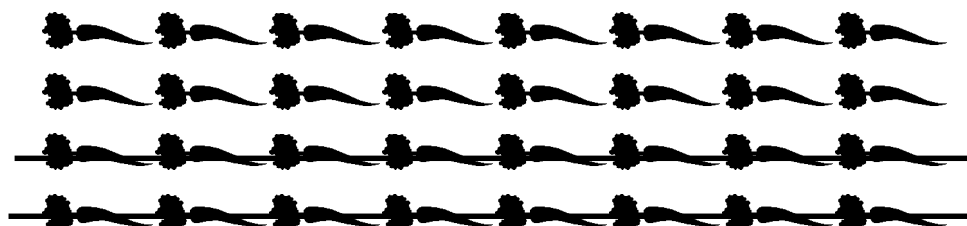
This skill can be very useful in helping a student visualise the problem, making it often easier to interpret and solve. In this case students would read over the problem, think about what it is asking and draw a diagram/picture to help them solve it.

Example:

A farmer planted four rows of eight carrots. If a quarter of the carrots didn't grow and a quarter were eaten by rabbits, how many carrots did the farmer have left?

Step 1: Read the problem and work out what it is asking?

Step 2: Draw four rows of eight carrots (or use lines to represent the carrots). Cross out a quarter (1 row) to show those that didn't grow and cross out another quarter or row to show the ones eaten by rabbits.



Step 3: Count up the number of carrots left and record the answer. (Answer = 16 carrots)

Teaching Points

Look for patterns

As with drawing a diagram or picture, looking for a pattern can also help students to visualise the problem. A pattern may present itself particularly in the areas of space and number.

Example:

A gardener wanted to make a path from his back door to the shed using at least two different shapes that have four or more sides. Suggest two different patterns the gardener could use and draw them on a piece of paper.

Step 1: Read the problem, and think about all the shapes that have two or more sides.

Step 2: Use shape blocks to create a few different patterns that only contain two shapes that have four or more sides.

Step 3: Select two different designs and draw them. Answers will vary from student to student, however, the shapes they would need to use could include: *square, rectangle, diamond, trapezium, parallelogram, pentagon, hexagon or octagon.*

Make a model

This strategy works particularly well when dealing with problems related to shape and space. Once again in order for students to visualise the problem it is often useful to construct it or make a model first. Materials such as blocks, 2D and 3D shapes, cubes, sticks, Plasticine, paper, popsticks, and so on are all handy in representing shapes and structures in our world.

Example:

Using shape blocks create a tower that is at least as high as your ruler and can support a school shoe. Which shapes work the best?

Step 1: Read the problem and visualise what it is asking.

Step 2: Gather various 3D shape blocks and begin working on a structure that is at least the height of your ruler and can support the weight of one of your school shoes.

Step 3: Compare the height of your tower to a ruler and test out its support by placing one of your shoes on its top.

Answer: *Answers will vary, however the most effective shapes would be rectangular prisms and cubes. The tower would also need to be wide enough to support the shoe.*

**TASK
9**

▶ SHAPE AND SPACE

CITY OF SHAPES

Materials: •pencil •ruler
•paper •computer (optional)

SELF
ASSESSMENT

1 What shapes are mainly used in houses and buildings? Make a list below.

2 Use the computer or a piece of paper to design a small city that is made up of buildings of many different shapes.

Challenge: Why do you think buildings need shapes with edges?

Indicator: Identifies where familiar shapes are used in everyday life.



**TASK
10**

▶ SHAPE AND SPACE

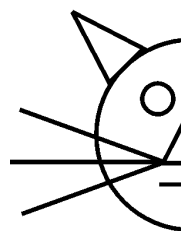
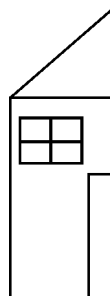
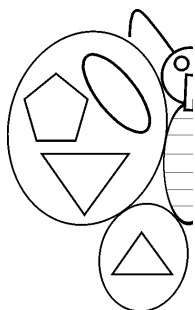
MISSING HALF

Materials: •paper •ruler •pencil

SELF
ASSESSMENT

Symmetrical means that when something is cut in half it is the same on each side.

1 Draw the missing half of the pictures below.



2 On a piece of paper draw a picture of a symmetrical robot made of squares, triangles, rectangles and circles.

Indicator: Uses shape and symmetry to complete and design simple pictures.

Challenge: Make a list of all the symmetrical things you can see in your classroom.



**TASK
17**

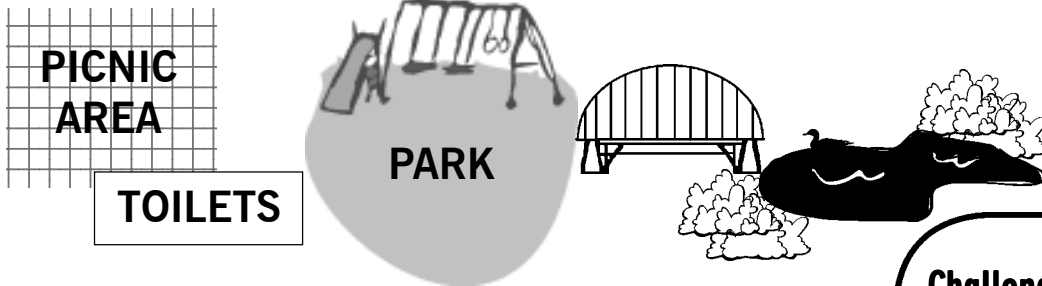
▶ SPACE (LOCATION)

CREATING PATHS

Materials: •pencils (red, blue, yellow) •grey lead pencil

SELF ASSESSMENT

- 1** Look at the park below. Draw in three different paths travelling from the picnic area to the duck pond. (Use a red, blue and yellow pencil.)



- 2** Which path do you think is the longest?

- 3** Which path do you think is the shortest?

Indicator: Creates different paths on a simple map.

Challenge:

Write a set of directions on how to get from your house to your local park if walking.

**TASK
18**

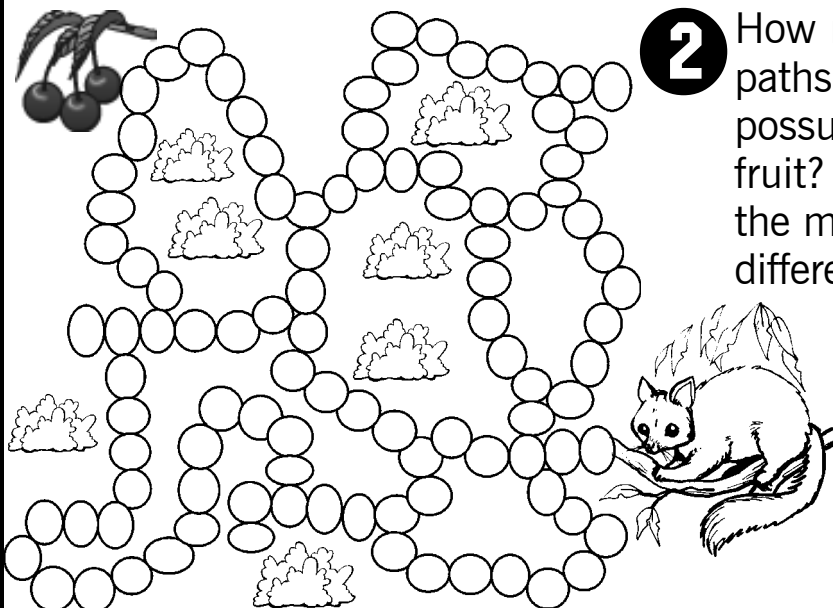
▶ SPACE (LOCATION)

POSSUM MAZE

Materials: •coloured pencils

SELF ASSESSMENT

- 1** Help the possum reach the fruit by drawing the shortest path through the bush maze.



- 2** How many possible paths could the possum take to the fruit? Draw them on the maze using different colours.



Challenge:

Design your own maze for an animal of your choice to reach its shelter. Give your maze to a friend to work out.

Indicator: Locates and follows different paths on a maze.

TASK
7

► NUMBER

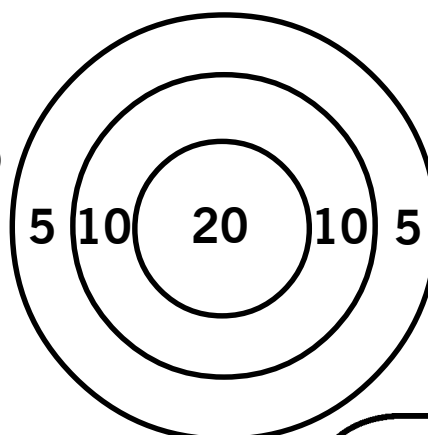
BALL TOSS

Materials: • pencil

SELF
ASSESSMENT



1 Look at the board and list the possible scores you could make if you had two balls that hit the board.



2 What would be the lowest and highest score you could make if you had three balls that hit the target?

a) lowest = _____ b) highest = _____

Indicator: Uses addition and multiplication facts to solve a problem.

Challenge:

What possible scores could you make if you had three balls that hit the board?

TASK
8

► NUMBER

BOWLING

Materials: • pencil

SELF
ASSESSMENT



1 In bowling you have two shots at knocking down 10 pins. List the different number combinations you could make if all pins got knocked down with each turn?

2 A *strike* is when all 10 pins are knocked down in one shot and equals 10 points. If a bowler made **3** strikes in the first three rounds, a **6** in the 4th round and a **9** in the 5th round, what would be his total pin score?

Indicator: Uses addition and multiplication facts to solve a problem.

Challenge: If a bowling card read "2 strikes, 7, 8, 9," what would the bowler's total score be?

**TASK
29**

► NUMBER

BEN'S CHORES

Materials: •pencil •coins

SELF
ASSESSMENT

1

Each time Ben completes a chore around the house his parents will give him \$1.00. How many chores must he complete to receive:

- a) \$3.00 b) \$8.00 c) \$15.00

2

If he has saved \$22.00, how many chores has he completed? _____

3

If he buys a fish bowl for \$9.00, a fish for \$3.00 and some fish food for \$2.00, how much money does he have left?

Challenge:

If Ben's older sister receives \$2.00 a chore, how many chores would she need to do to save \$22.00?

Indicator: Adds, multiples and divides money to solve a problem.



**TASK
30**

► NUMBER (MEASUREMENT)

CAKE SHOP

Materials: •pencil

SELF
ASSESSMENT

1

If a whole cake costs \$12.00, how much will the following cost:

- a) $\frac{1}{2}$ cake? b) $\frac{1}{4}$ cake? c) $\frac{1}{3}$ cake?

2

If the cake was divided into six slices, how much would each slice cost?

3

If the cake was divided into 12 slices, how much would five slices cost?

Challenge: If the cake was divided into eight slices, how much would:

- a) one slice cost?
b) six slices cost?

Indicator: Uses knowledge of money and fractions to solve a problem.



TASK 11

► MEASUREMENT

THREE BEARS

Materials: •pencil •tape measure

SELF ASSESSMENT



1

Make a list of the differences you think there are between the three bears (from *Goldilocks and the Three Bears*).

DADDY BEAR	MUMMY BEAR	BABY BEAR

2

You need to make three doors. If Daddy bear is 180 cm tall, Baby bear is half Daddy's height and Mummy is in the middle, how large should you make each door?

- a) Daddy's door ____ b) Mummy's door ____
 c) Baby's door ____

Indicator: Makes comparisons between the sizes of two or more objects.

Challenge:

Suppose you had to make a door that only students in your class would use. How would you work out how high to make this door? What would the height need to be?

TASK 12

► MEASUREMENT

LEAKING TAPS

Materials: •pencil

SELF ASSESSMENT



1

If a tap lost 10 drops of water every minute, how many drops would it lose after:

- a) 3 minutes? b) 6 minutes? c) 9 minutes?

2

If a bath lost $\frac{1}{2}$ cup of water in five minutes, how much would it lose after:

a) 10 minutes?

b) 20 minutes?

c) 30 minutes?

Indicator: Uses knowledge of volume, fractions and time to solve a problem.

Challenge:

How long would it take the bath to lose five cups of water?

TASK 5

► CHANCE

HOW MANY JELLY BEANS?

Materials:
•pencils

SELF ASSESSMENT

1

A jam jar was filled with jellybeans for a guessing competition. Look at the jar and the children's guesses, predict who you think would most likely and least likely win.



- Sarah – 12 •James – 30 •Ben – 6
- Lucy – 75 •Megan – 10 •John – 21
- Adam – 9 •Simone – 18 •Harry – 50

Most likely: _____ Least likely: _____

2

If it cost 20c a guess, how much money did they raise? _____

3

What prize do you think the winner would receive? _____

Challenge:
Invent and describe your own chance competition.

Indicator: Predicts what might happen in simple chance experiments.

TASK 6

► CHANCE/NUMBER

BEANBAG TOSS

Materials: •pencils

SELF ASSESSMENT

1

At the school fete one of the stalls was the beanbag toss where \$1.00 buys two beanbags which are then thrown into a bucket to win a prize. Look below at how many bean bags the children purchased and number them **1** to **6** from having the best to least chance of winning.

- a) Alex (10) _____ b) Jake (6) _____ c) Megan (12) _____
- d) Oliver (4) _____ e) Emily (8) _____ f) Michelle (2) _____



2

How much did each child spend at the beanbag toss?

- a) Alex – \$ _____ d) Oliver – \$ _____
- b) Jake – \$ _____ e) Emily – \$ _____
- c) Megan – \$ _____ f) Michelle – \$ _____

Challenge:
How much money was collected altogether from these six children?

Indicator: Predicts and calculates what might happen in a simple game of chance.